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# THE EFFICIENCY OF MODIFIED JACKKNIFE AND RIDGE TYPE REGRESSION ESTIMATORS:

#### COMPARISON

Feras Sh . M . Batah , Thekke V . Ramanathan and Sharad D . Gore

Abstract . A common problem in multiple regression models is multicollinearity , which produces undesirable effects on the least squares estimator . To circumvent this problem , two well known estimation procedures are often suggested in the literature . They are Generalized Ridge Regression parenleft — eight G-bracketrightn-R-aR-d)h — es — e ti a — m — Ja — ct — ki-kon—ns — ed — u g R — gi-es-dg-t e e — db — Re-ye — r — Ho-ss-ei-rl — on — aparenleft — nJ — dR — K — Reparenright—n nard [ one — es — threebracketright — ti-periodT-mah — te — ioG-ns — R u R — ge — ge-st-st-im—e d b — to-y-in — Sile-ng-ad e t — t a a — l. [ e d u t — i on nt e — h sa mpling variance , whereas , JRR leads to a reduction in the bias . In this paper , we propose a new estimator namely , Modified Jackknife Ridge Regression Estimator (MJR) . It is based on the criterion that combines the ideas underlying both the GRR and JRR estimators . We have investigated standard properties of this new estimator . From a simulation study , we find that the new estimator often outperforms the LASSO , and it is superior to both GRR and JRR estimators , using the mean squared error criterion . The conditions under which the MJR estimator is better than the other two competing estimators have been investigated .

F ull text

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Department of Statistics , University of Pune , India . e - mail : sdgore @ stats . unipune . ernet . in Surveys \*in Mathemati \* and it\* s Appli\*cati\* ons  $3*(*2**0_0^**_8^*)$ , 111-122 h t tp : //w w w . u t gj i u . r o / m a t h / sm a